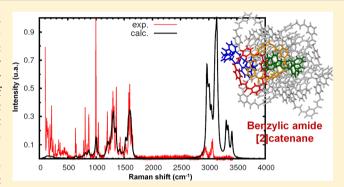


# Assignment of the Raman Spectrum of Benzylic Amide [2] Catenane: Raman Microscopy Experiments and First-Principles Calculations

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Supporting Information

**ABSTRACT:** In this work, we use Raman spectroscopy and quantum first-principles calculations to unveil the experimental spectrum of a complex molecular solid-like benzylic amide [2] catenane, a representative example of a mechanically interlocked molecular architecture. We use large-scale density functional theory calculations to obtain the complete set of vibrational normal modes of the catenane crystal, whose unit cell contains 544 atoms. Subsequently, we demonstrate that these calculations are able to accurately reproduce the experimental Raman spectrum of this molecular compound, without introducing any empirical corrections or fittings in the calculated eigenfrequencies. Thanks to the good agreement between the experimental and theoretical spectra, it is possible



to carry out the complete assignment of the main vibrational modes responsible for the whole spectrum. A detailed description in terms of the usual internal coordinates is given for all of these representative modes. This description, rather difficult from the experimental point of view, provides valuable information about the molecular structure of this compound, compatible with experimental evidences reported in the literature.

## 1. INTRODUCTION

The main mechanically interlocked molecular architectures were known since the middle of the 20th century. They are compounds whose molecular subunits are linked mechanically as a consequence of their topology instead of traditional chemical bonds. However, it was not until the early 90's when the pioneering work by B. L. Feringa, J. P. Sauvage, and J. F. Stoddart gave rise to the so-called template-directed syntheses based on the preorganization of the reactants through noncovalent interactions. Thanks to this breakthrough, a precise control in the final cyclization reactions of the macrocyclic precursors was achieved, leading to the efficient production of hundreds of mechanically interlocked compounds such as catenanes, rotaxanes, and molecular knots.2,3

Compounds owning mechanical bonds display peculiar chemical properties distinctive from those of typical covalent materials. In particular, the incorporation of moieties with molecular recognition motifs opens the door to the possibility of building and designing artificial molecular machines at atomic level.4,5 For this reason, this class of materials is of extreme importance and, at the same time, represents a challenge from the characterization point of view (both theoretical and experimental). This is due to their complex

structure and the internal freedom of their building blocks, which includes the ability of the rings to rotate with respect to one another and other low-energy dynamic processes. This motion can be detected and measured by magnetic nuclear resonance spectroscopy.<sup>6,7</sup>

In this work, we focus on the benzylic amide [2]catenane, a representative example of a large family of molecules, first synthesized in 1995 through a self-assembly procedure.<sup>8,9</sup> It is one of the simplest [2]catenanes, constituted by two identical macrocycles that are mechanically interlocked. Each of them, in turn, is formed by four bound aromatic units (-C<sub>6</sub>H<sub>4</sub>- $CO-NH-CH_2-)$  or  $(-C_6H_4-CH_2-NH-CO-)$ , linked in meta or para positions, as depicted in Figure 1. This compound has been extensively characterized by a number of different experimental techniques, including X-ray diffraction, magnetic nuclear resonance spectroscopy, 5,9,10 X-ray photoelectron spectroscopy, <sup>11</sup> electron energy loss spectroscopy, <sup>12</sup> vibrational spectroscopy, <sup>13</sup>, <sup>14</sup> or inelastic neutron scattering. <sup>15</sup> In addition, the internal dynamics of this catenane has also been investigated with classical molecular dynamics, 6,13,16,17 paying

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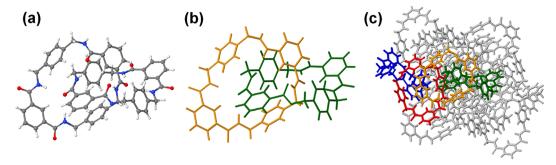


Figure 1. Molecular and crystal structure of the benzylic amide [2] catenane: molecular structure as embedded in the crystal structure, ball-and-stick model (a) and two-color simplified model showing the two different macrocycles (b). Crystal packing of the molecules in the crystalline state (c). Some macrocyclic units are highlighted in colors to ease the visualization.

special attention to the rotation of the rings. These studies reveal that the benzylic amide [2]catenane is very sensitive to its chemical environment as a consequence of the presence of strong polar groups C=O and N-H capable to interact with different external species via hydrogen bonds. 10,14

In this work we aim to study the vibrational spectrum of this catenane using a combination of Raman microscopy experiments and quantum first-principles calculation. Unlike earlier studies, 13,14,16 in which the quantum description of such a large and complex molecular solid was unaffordable from the computational point of view, we use calculations based on density functional theory to determine both the vibrational modes of the catenane crystal and their Raman intensities. So far, this kind of analysis at quantum level had been restricted to those systems with smaller unit cells, mainly inorganic compounds. 18-22 However, in the present work, we disclose the Raman spectrum of such a complex molecular solid, finding a very good agreement between the theoretical calculations and the experimental results. This fair agreement allows us to perform a complete assignment of all of the peaks appearing in the experimental Raman spectrum, providing the corresponding geometric description of the relevant modes. Therefore, the interest of this work is twofold. On the one hand, our study devises a simple procedure to accurately determine the vibrational spectrum of large systems containing hundreds of atoms in the unit cell. Besides, it is a general method, applicable either for molecules or crystalline solids. On the other hand, it represents a significant progress in Raman spectroscopy, where often the extraction of molecular-scale features of a complex material by spectra analysis might be rather difficult. Because most of the relevant Raman active modes have been properly assigned, these results will shed new light in further studies involving related molecular systems.

## 2. EXPERIMENTS

**2.1. Synthesis.** The synthesis of the benzylic amide [2] catenane [i.e., IUPAC name [2] (1,7,14,20-tetraaza-2,6,15,19-tetraoxo-3,5,9,12,16,18,22,25-tetrabenzocyclohexacosane)-(1',7',14',20'-tetraaza-2',6',15',19'-tetraoxo-3',5',9',12',16',18',22',25'-tetrabenzocyclohexacosane) catenane] was carried out following the method described in ref 13. Triethylamine [0.921 g (14.627 mmol)] was dissolved in 100 mL of anhydrous chloroform, and stirred for half an hour in an argon atmosphere in a three-neck angled round-bottom flask. Then, 0.665 g (3.286 mmol) of *p*-xylylene diamine and 0.447 g (3.313 mmol) of isophthaloyl chloride were dissolved in two flasks containing 100 mL of anhydrous chloroform each one. These solutions were transferred into two isobaric funnels,

and both were attached to the three-neck round flask. The solutions were mixed simultaneously for half an hour. The resulting solution was kept in agitation for 24 h. Later, the solution was washed with 3  $\times$  100 mL of HCl (1 M) and 3  $\times$  100 mL of NaOH (1 M). The organic layer was dried with magnesium sulfate, and the solvent in this layer was evaporated in a rotary evaporator. Around one-half of the final product was recrystallized in order to obtain crystals large enough to facilitate their study by micro-Raman ( $\mu$ -Raman). For this purpose, we dissolved the product in methanol and acetone and left it in a crystallizer for a week.

To confirm that we got the desired catenane, solution nuclear magnetic resonance (NMR) spectra were recorded on Bruker DRX 400 (9.4 T, 400.13 MHz for  $^1\mathrm{H}$  and 100.62 MHz for  $^{13}\mathrm{C}$ ) using a 5 mm QNP direct-detection probehead equipped with a z-gradient coil, at 300 K. Chemical shifts ( $\delta$  in ppm) are given from internal solvent, DMSO- $d_6$  2.49 for  $^1\mathrm{H}$  and 39.5 for  $^{13}\mathrm{C}$ . We got for  $^1\mathrm{H}$  NMR  $\delta$  = 8.47 (8H, s), 7.95 (4H, d), 7.80 (8H, d), 7.41 (4H, t), 6.65 (16H, s) and 3.92 (16H, s). For  $^{13}\mathrm{C}$  NMR, we got  $\delta$  = 165.8, 137.2, 134.2, 129.6, 128.2, 126.6 and 42.8. These results are consistent with those of previous works.

2.2. Raman Spectroscopy. The equipment used was a Jobin Yvon spectrophotometer model LabRam-IR HR-800 with a focal length of 800 mm, a grating of 1800 grooves mm, confocal pinhole set at 100 µm, and a Peltier refrigerated charge-coupled device (1024 × 256 pixels). These conditions and excitation with the 632.8 nm line of a He/Ne laser give rise to an average spectral resolution of 1 cm<sup>-1</sup> in the wavenumber range of 100-1700 cm<sup>-1</sup>. The sine bar linearity of the spectrograph was adjusted using the fluorescent lamps of the laboratory (zero-order position) and the lines at 640.22 and 837.76 nm of a Ne lamp. The spectrophotometer was coupled to an Olympus BX41 confocal optical microscope. The confocality of the instrument was refined using the 519.97 cm<sup>-1</sup> line of a silicon wafer. The laser effective power at the sample position using 50× and 100× objectives was kept at 250 and 225  $\mu$ W, respectively, in order to avoid sample alteration. The indicated conditions result in a lateral resolving power of  $\sim 1-2 \mu m$  (100× objective lens) and  $\sim 5 \mu m$  (50× objective lens) at the specimen. Wavenumber shift calibration<sup>23</sup> with 4-acetamidophenol, naphthalene, and sulfur in the 150-3100 cm<sup>-1</sup> range using the same recording conditions resulted in a mean deviation of  $\Delta \nu_{\rm cal}$  –  $\Delta \nu_{\rm obs}$  = 0.96  $\pm$  0.75  ${\rm cm}^{-1}$  ( $t_{\rm Student}$  of 95%). The spectral integration time was 20 s, and 20 records were accumulated in order to achieve spectra with an acceptable signal-to-noise ratio.

Depolarized Raman spectra of a large series of microcrystals of the synthesized catenane have been collected. Raleigh line filter decay at low Stokes wavenumber has been baselinecorrected using the Multi-Point algorithm (option "Level + Zero") of the Grams/AI v. 7.00 software, choosing around 10 points in each spectrum. No other numerical treatment or correction (smoothing, shifting, deconvolution, etc.) has been applied to the spectra.

## 3. FIRST-PRINCIPLES CALCULATIONS

In this work, we have characterized the benzylic amide [2] catenane crystal by means of density functional theory (DFT) calculations using the VASP (Vienna Ab initio Simulation Package) code. A plane-wave basis sets with a cutoff of 400 eV was used together with PAW pseudopotentials<sup>25,26</sup> for all involved species (C, N, O, and H). The Perdew–Burke–Ernzerhof functional<sup>27</sup> was employed to reproduce the electronic exchange and correlation interactions supplemented with the semiempirical D3 correction by Grimme, <sup>28</sup> to account for possible dispersion interactions.

A good equilibrium geometry for the catenane crystal was obtained combining electronic self-consistent loops (cutoff 10<sup>-6</sup> eV) with a conjugate gradient optimization of the structure, until forces upon atoms were less than 0.005 eV/Å. This strict criterion is imposed to ensure the success of the subsequent normal mode analysis. During the ionic relaxation, the lattice constants were kept fixed in order to preserve the original symmetry of the crystal structure and the reciprocal space was sampled with a  $2 \times 2 \times 2$  Monkhorst-Pack grid<sup>29</sup> because of the large size of the unit cell. The starting geometry was obtained from X-ray crystallographic data<sup>8,30</sup> (see Figure 1c). This is an orthorhombic unit cell (a = 17.4382 Å, b =12.4628 Å, c = 23.6926 Å, space group *Pbcn*), which contains four catenane molecules, leading to  $136 \times 4 = 544$  total atoms per unit cell. Periodic boundary conditions are used to properly reproduce the crystal structure of the solid-state

The normal mode analysis was carried out by direct diagonalization of the Hessian matrix according to the classical analysis.31,32 Under the harmonic approximation, the vibrational eigenmodes of a system constituted by N atoms are obtained after solving the corresponding eigenvalue problem

$$\sum_{j=1}^{3N} (f_{jk} - \lambda_{(n)} \delta_{jk}) A_{j,(n)} = 0$$
(1)

where  $f_{ik}$  is the mass-weighted Hessian matrix,  $\lambda_{(n)} = (2\pi\nu_n)^2$  is the eigenvalues, related to the frequencies  $\nu_n$  of the nth mode, and  $A_{j,(n)}$  is the elements of the corresponding eigenvectors. The Hessian matrix is numerically obtained through finite differences by computing the second derivatives of the energy with respect to the atomic positions. Six different displacements (±0.02 Å) per atom along the three Cartesian components are used in this algorithm. Notice that only those atoms belonging to the unit cell are considered in this calculation, giving rise to a total of  $544 \times 3 - 6 = 1626$  normal modes. This procedure to calculate vibrational normal modes was tested with the benzamide molecule, closely related to structural building blocks of the catenane. A fair agreement with previous calculations and experimental Raman and infrared spectra<sup>33</sup> was found. See Table S1 in the Supporting Information for further details.

The estimation of Raman intensities was carried out according to the scheme suggested by D. Porezag and M. R. Pederson. 34 In this approach, the scattered intensity  $I_n$  by the nth mode can be computed in terms of the variation of some elements  $(\alpha_{ii})$  of the polarizability tensor along that vibrational mode. In order to mimic our experimental conditions, we have to use this equation<sup>3</sup>

$$I_n \propto \frac{1}{45} \left[ 45 \left( \frac{\mathrm{d}\alpha}{\mathrm{d}Q} \right)_{\mathrm{eq}}^2 + 7 \left( \frac{\mathrm{d}\beta}{\mathrm{d}Q} \right)_{\mathrm{eq}}^2 \right]$$
 (2)

where  $\alpha$  and  $\beta$  are two invariants of the polarizability tensor

$$\alpha = \frac{1}{3}(\alpha_{11} + \alpha_{22} + \alpha_{33}) \tag{3}$$

$$\beta^{2} = \frac{1}{2} [(\alpha_{11} - \alpha_{22})^{2} + (\alpha_{11} - \alpha_{33})^{2} + (\alpha_{22} - \alpha_{33})^{2} + 6(\alpha_{12}^{2} + \alpha_{13}^{2} + \alpha_{23}^{2})]$$
(4)

The above expression is chosen because it is compatible with our experimental setup of Raman microscopy, in which nonpolarized light is used as an excitation source and the backscattered radiation (180°) is detected, leading to a depolarization ratio equals to one. Therefore, two additional calculations per mode must be carried out in order to determine the Raman intensity of each vibrational mode. Because of the large size of the system, these calculations are restricted solely to the  $\Gamma$  point in the reciprocal space. In these calculations, the polarizability tensor is calculated 36,37 in two different geometries slightly displaced along the corresponding normal model with respect to the equilibrium position. In this way, the derivatives of eq 2 can be evaluated to obtain the Raman intensity. Finally, a discrete collection of scattered intensities associated with each normal mode is obtained and the complete spectrum can be constructed by fitting each eigenfrequency to Lorentzian distributions according to

$$F_n(\nu; I_n, \nu_n, \gamma) = \frac{I_n}{\pi} \frac{\gamma}{(\nu - \nu_n)^2 + \gamma^2}$$
 (5)

where  $\gamma$  was set to  $10^{-3}$  cm<sup>-1</sup> in order to achieve a good resolution.

## 4. RESULTS AND DISCUSSION

Following the synthetic procedure introduced in section 2, we obtained several samples after the recrystallization process. The obtained crystals display a grain size distribution between 10 and 30  $\mu$ m. They present a number of different morphologies because of their different spatial orientations and also to the appearance of different crystalline defects, such as crystal twinning. In order to achieve the highest reliability degree in the experimental measurements, many different crystals were analyzed by  $\mu$ -Raman, including the most representative shapes found in the samples. In Figure 2, we have selected four of them. S1 corresponds to the amorphous catenane without further recrystallization, S2 has a rectangular shape, S3 a rhombic one, and S4 is rectangular-shaped. Because Raman microscopy allows us to analyze each individual crystal by focusing the laser beam appropriately, the exact measured points are indicated in each case with a red cross in Figure 2.

As a result, four different Raman spectra were selected fulfilling the highest quality criteria (i.e., high peak resolution, The Journal of Physical Chemistry C

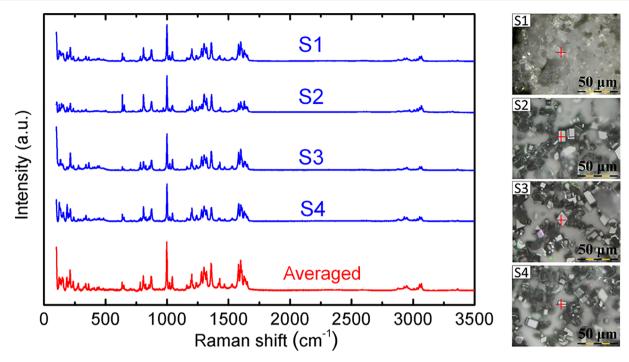
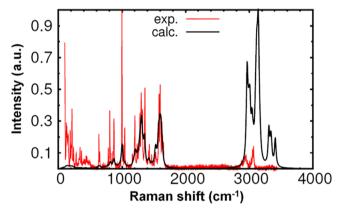


Figure 2. Raman spectra (S1–S4 and averaged) of several crystals of benzylic amide [2] catenane with different shapes, according to the microphotographs shown in the right panel. These microphotographs were made with an LWD eyepiece  $(50\times)$ , and the exact location where the spectra were recorded is depicted with a red cross.

good signal/noise ratio, large enough intensities, etc.). They are shown (blue lines) in the left panel of Figure 2 and are labeled as S1-S4, according to each microphotography. None of the spectra has been refined except for the removing of the Rayleigh contribution by subtracting the baselines. All of these spectra were carefully analyzed in order to assign the proper location of all observed peaks, revealing that all of them are rather similar and essentially display the same features, in good agreement with previous results reported in the literature. 13 Notice that, slight differences in the intensity of some peaks are found due to the different relative orientations of each crystal with respect to the incident radiation of the laser beam and also the crystallinity degree. To overcome this issue, an averaged spectrum (red line) was obtained and it will be selected for further comparisons with the theoretical calculations. As expected this averaged spectrum resembles very much to S1, obtained from the amorphous sample without recrystallization. This fact reveals that the Raman fingerprint of this compound is essentially related to their molecular features and not to the long-range symmetry.

Theoretical calculations were carried out according to the approach detailed in section 3. Figure 3 shows the comparison between the theoretical Raman spectrum obtained with DFT calculations (black line) and the experimental spectrum (red line), the averaged one. We have chosen the averaged spectrum because the theoretical calculation assumed a random distribution of the sample dipoles with respect to the incident electromagnetic field, which is not the case in our  $\mu$ -Raman experiments of single crystals. As already mentioned, this circumstance can be compensated by averaging over different spectra. Even so, we cannot expect, in this respect, a perfect agreement throughout the whole spectrum as a consequence of the intrinsic limitations of eq 2, used to calculate the Raman intensity. We cannot forget that this expression is the result of a relatively simple approximation



**Figure 3.** Comparison between the calculated Raman spectrum (black line) and the experimental averaged spectrum (red line) obtained by  $\mu$ -Raman.

based on a first-order approach. Therefore, we find a clear overestimation of the intensities in the high wavenumber shift region (>2900 cm<sup>-1</sup>). Conversely, this is not the case in the low wavenumber shift region where some intensity differences are expected due to the remaining Rayleigh contribution to the total intensity in the experimental spectrum, which is completely absent in the calculations. However, the agreement between both spectra is remarkable regarding the matching of the peak locations, especially taking into account that no rescaling fittings have been applied to the obtained eigenfrequencies. This result reveals a high accuracy in the determination of the vibrational normal modes of the catenane crystal. Furthermore, we will see that the discrepancies found in the intensities can be drastically reduced if different regions of the spectrum, belonging to different kinds of normal modes, are considered separately.

Once we have checked the good agreement between calculations and experiments, we are in a position to assign the different vibrational modes corresponding to the experimental peaks of the spectrum. This theoretical assignment adds valuable information about the molecular structure of the compound, providing a geometrical description of those vibrational modes responsible for the experimentally observed peaks in the spectra. However, for such a complex case like benzylic amide [2] catenane, this is not an easy task because of the large number of degrees of freedom. In particular, 544 atoms per unit cell lead to a total of 1626 normal modes, although only a fraction of them will really contribute with a significant activity to the Raman spectrum. In order to select these more active modes, we proceed by imposing some cutoffs for the intensity displayed by a given mode. In this way, only those modes with an intensity larger than the chosen cutoff (expressed with respect to the most intense mode) were selected for further analysis. Two different optimized values of cutoff were selected throughout the spectrum fulfilling two opposed requirements: they have to be low enough to minimize the number of active modes but, at the same time, large enough to keep the shape of the peaks displayed in the whole spectrum. With these criteria, we retained 34 modes in the medium wavenumber shift region (between 600 and 1700 cm<sup>-1</sup>) and 23 modes in the high wavenumber shift part (>2900 cm<sup>-1</sup>), using  $\sim$ 25% and  $\sim$ 50% of the maximum intensity as cutoff values, respectively. Thank to this procedure, it is possible to carry out the complete assignment of the main vibrational modes responsible for the whole spectrum and the subsequent comparison with the experimental results. This is what is made in Table 1, where the complete mode list, together with a brief geometrical description of each one in terms of usual internal coordinates is given with the associated peaks in both the theoretical and experimental spectra. Notice that the assignment in the low wavenumber shift region (<600 cm<sup>-1</sup>) is much more complex, and it has not been included in Table 1.

The comprehensive assignment collected in Table 1 discloses the Raman fingerprint of this compound in terms of different kinds of vibrations of the catenane crystal. Before a deeper analysis, it is worth noting that a single peak in the experimental spectrum might be a complex overlap of several modes and thus, its location may not exactly coincide with any normal mode. In addition, because of the crystal symmetry, there is a number of degenerate modes, which are equivalent and localized in different but equivalent groups of the unit cell (i.e., aromatic rings, carbonyl groups, etc.). In any case, it has been possible to assign every peak of the experimental spectrum to one or several discrete modes of the theoretical calculation. To get further insight of the spectrum, we have divided the wavenumber shift range in four different regions associated with characteristic vibrations: (i) [0, 600] cm<sup>-1</sup>, (ii) [600, 1100] cm<sup>-1</sup>, (iii) [1100, 1700] cm<sup>-1</sup>, and (iv) [2900, 3500] cm<sup>-1</sup>. As usual, the empty region between 1700 and 2900 cm<sup>-1</sup> has been discarded for further analysis because it lacks of any relevant Raman fingerprint, as shown in Figures 2 and 3. In Figure 4, we show the decomposed Raman spectrum in these four regions compared with the theoretical calculation. Notice that in each region, both spectra have been renormalized using the strongest line of each region, leading to a remarkable overall agreement also in the relative intensities. A different version of Figure 4 can be found in

Table 1. Comparison between the Main Peaks of the Experimental Raman Spectrum and Those of the Theoretical Calculation<sup>a</sup>

(No.)   (No	————— Peaks	$(cm^{-1})$	Mode	$\nu_n$	Description
1126   666   sour-of-plane-rd + πCNCC     1874   874   921   874   sin-plane-rd + πCNCC + s-t-νCH     1875   1001   sin-plane-rd + s-t-νCH     1876   1004   sin-plane-rd + s-t-νCH     1878   1004   sin-plane-rd + s-t-νCH     1879   1011   788   1004   sin-plane-rd + s-t-νCH     1870   1213   619   1211   sin-plane-rd + s-t-νCH     1870   1316   637   1305   6CCN + a-in-plane-rd     1870   1370   6CCN + a-in-plane-rd     1870   1371   6CCN + a-in-plane-rd     1870   1349   481   1344   6CCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1340   431   1354   wCH2 + δCCN + a-in-plane-rd     1870   1340   431   1354   wCH2 + δCCN + a-in-plane-rd     1870   1341   1352   νCN + νCC     1870   1342   VCN + δCCN + a-in-plane-rd     1870   1343   1375   νCC + νCO + δCNC + a-in-plane-rd     1870   1343   1375   νCC + νCO + δCNC + a-in-plane-rd     1870   1344   1354   νCO + νCN + δCNC + a-in-plane-rd     1870   266   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + νCN + α-in-plane-rd     1870   276   1361	(exp.)	(calc.)	(No.)		-
1126   666   sour-of-plane-rd + πCNCC     1874   874   921   874   sin-plane-rd + πCNCC + s-t-νCH     1875   1001   sin-plane-rd + s-t-νCH     1876   1004   sin-plane-rd + s-t-νCH     1878   1004   sin-plane-rd + s-t-νCH     1879   1011   788   1004   sin-plane-rd + s-t-νCH     1870   1213   619   1211   sin-plane-rd + s-t-νCH     1870   1316   637   1305   6CCN + a-in-plane-rd     1870   1370   6CCN + a-in-plane-rd     1870   1371   6CCN + a-in-plane-rd     1870   1349   481   1344   6CCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1349   481   1344   wCH2 + δCCN + a-in-plane-rd     1870   1340   431   1354   wCH2 + δCCN + a-in-plane-rd     1870   1340   431   1354   wCH2 + δCCN + a-in-plane-rd     1870   1341   1352   νCN + νCC     1870   1342   VCN + δCCN + a-in-plane-rd     1870   1343   1375   νCC + νCO + δCNC + a-in-plane-rd     1870   1343   1375   νCC + νCO + δCNC + a-in-plane-rd     1870   1344   1354   νCO + νCN + δCNC + a-in-plane-rd     1870   266   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1367   νCC + νCO + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + a-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + α-in-plane-rd     1870   276   1361   νCC + νCN + δCNC + νCN + α-in-plane-rd     1870   276   1361	636		1146	638	a-in-plane-rd + r-\nuCH
Second		641			
1940   874   921   874   sin-planerd + πCNCC + δHCH     1999   1001   788   1004   sin-planerd + s-r-νCH     186   1004   sin-planerd + s-r-νCH     186   1004   sin-planerd + s-r-νCH     187   1004   sin-planerd + s-r-νCH     187   1004   sin-planerd + s-r-νCH     188   1004   sin-planerd + s-r-νCH     180   1211   sin-planerd + s-r-νCH     180   1211   sin-planerd + δCCN     1282   570   1267   δCCN + a-in-planerd     180   1306   537   1305   δCCN + a-in-planerd     180   1310   532   1306   δCCN + a-in-planerd     180   1310   333   1359   νCCN + a-in-planerd     180   1310   333   1359   νCN + δCCN     181   1348   δCCNC     1330   1331   333   1329   νCN + νCC     1331   333   1529   νCN + νCC     1332   333   1529   νCN + νCC     1582   303   1575   νCC + sin-planerd     1594   1294   362   νCC + νCO + δCNC + a-in-planerd     1595   1295   1392   νCC + νCO + δCNC + a-in-planerd     1596   1296   1392   νCC + νCO + δCNC + a-in-planerd     1597   1296   1397   νCC + νCO + δCNC + a-in-planerd     1598   1296   1392   νCO + νCC + δCNC + a-in-planerd     1599   1296   1392   νCO + νCC + δCNC + a-in-planerd     1590   1297   1398   1399   1399     1591   1391   1391   1391   1391   1391     1592   1393   1391   1391   1391   1391   1391     1593   1394   1391   1391   1391   1391   1391     1594   1395   1391   1391   1391   1391   1391   1391   1391     1595   1392   1391	808	815			
1999   1001   788   1004   sin-planerd + s-r-νCH   789   1001   sin-planerd + s-r-νCH   786   1004   sin-planerd + s-r-νCH   786   1004   sin-planerd + s-r-νCH   785   1267   sin-planerd + s-r-νCH   785   1267   sin-planerd + s-r-νCH   785   1267   sin-planerd   sin-p					
999 1001 788 1004 sin-plane-rd + s-r-νCH   785 1004 sin-plane-rd   785 1004 sin-plane-rd + s-r-νCH   785 1004 sin-plane-rd					
101	000	1001			-
1044   1033   756   1044   s-in-planer-d + s-r-νCH     1044   1033   756   1044   δCNC + νCN + s-in-planer-d     1048   1033   756   1044   δCNC + νCN + s-in-planer-d     1040   1213   619   1211   s-in-planer-d + δCCN     1282   570   1267   δCCN + a-in-planer-d     1301   1306   537   1305   δCCN + a-in-planer-d     1306   537   1305   δCCN + a-in-planer-d     1306   537   1305   δCCN + a-in-planer-d     1307   1308   4311   δCCN + a-in-planer-d     1308   4311   1317   rCCNC     1319   431   1318   δCCNC     1320   1349   431   1348   δCCNC     1330   1531   333   1529   νCN + νCC     1340   1575   νCC + s-in-planer-d   νCO     1582   266   1592   νCO + νCO + δCNC + a-in-planer-d     1599   1597   261   1610   νCC + νCO + δCNC + a-in-planer-d     1599   1297   261   1610   νCC + νCN + δCCN + s-in-planer-d     1628   236   1625   νCO + νCN + δCCN + s-in-planer-d     1628   236   1625   νCO + νCN + δCCN + s-in-planer-d     1628   231   1620   νCO + νCN + δCCN + s-in-planer-d     1628   232   1634   νCO + νCN + δCCN + s-in-planer-d     1629   2406   s-νCH2 + δCCN + s-in-planer-d     1629   2406   s-νCH2 + δCCN + νCO + δCCN + s-in-planer-d     1629   2406   s-νCH2 + δCCN + νCO + νCN + δCN + s-in-planer-d     1620   2409   s-νCH2 + δCCN + νCO + νCN + δCN + s-in-planer-d     1621   2409   2406   s-νCH2 + δCCN + νCO + νCN + δCN + νCO + νCN + δCN + s-in-planer-d     1622   2409   s-νCH2 + δCCN + νCO + νCN + δCN + s-in-planer-d     2410					·
1044   1033   756   1044   5CNC + $\nu$ CN + s-in-planerd   6CNC   1208   s-in-planerd + $\delta$ -CCN   622   1208   s-in-planerd + $\delta$ -CCN   1213   622   1208   s-in-planerd + $\delta$ -CCN   1282   570   1267   $\delta$ -CCN + a-in-planerd   $\delta$ -CCN   1282   538   1287   $\delta$ -CCN + a-in-planerd   $\delta$ -CCN + $\delta$ -CCN   $\delta$ -CCN + $\delta$ -CCN + $\delta$ -CCN   $\delta$ -CCN + $\delta$	555				
1044   1033   756   1044   δCNC + $\nu$ CN + $\nu$ CN + sin-planerd     1202   1213   619   1211   sin-planerd + δCCN     1282   570   1267   δCCN + a-in-planerd     1306   537   1305   δCCN + a-in-planerd     1301   1306   537   1305   δCCN + a-in-planerd     1302   1349   491   1348   δCCNC     1362   1349   491   1348   δCCNC     1370   1371   δCCN + δCCN     1381   1351   1352   $\nu$ CN + $\nu$ CC     1382   1394   491   1348   δCCNC     1383   1523   $\nu$ CN + $\nu$ CC     1384   1529   $\nu$ CN + $\nu$ CC     1385   1331   1529   $\nu$ CN + $\nu$ CC     1582   303   1575   $\nu$ CC + $\nu$ CC + $\nu$ CN + a-in-planerd     1597   266   1592   $\nu$ CC + $\nu$ CO + $\nu$ CN + a-in-planerd     1598   1597   $\nu$ CC + $\nu$ CC + $\nu$ CCN + a-in-planerd     1628   236   1625   $\nu$ CC + $\nu$ CC + $\nu$ CCN + a-in-planerd     1628   236   1625   $\nu$ CC + $\nu$ CC + $\nu$ CCN + $\nu$ CCN + $\nu$ CCN + a-in-planerd     1628   243   1620   $\nu$ CO + $\nu$ CC + $\nu$ CCN + $\nu$ CCN + $\nu$ CN + $\nu$					•
1202   1213   622   1208   s-in-plane-rd + δCCN     1282   570   1267   δCCN + a-in-plane-rd     1287   558   1287   δCCN + a-in-plane-rd     1288   558   1287   δCCN + a-in-plane-rd     1306   537   1305   δCCN + a-in-plane-rd     1306   532   1306   δCCN + a-in-plane-rd     1322   519   1317   τCCNC     1322   491   1348   δCCNC     1349   441   1354   ωCH2 + δCCN + a-in-plane-rd     1323   1349   441   1354   ωCH2 + δCCN     1330   1531   333   1529   νCN + νCC     1330   1531   333   1529   νCN + νCC     1330   1575   νCC + δCCN + in-plane-rd     1482   286   1592   νCC + νCO + δCNC + a-in-plane-rd     1594   286   1592   νCC + νCO + δCNC + a-in-plane-rd     1595   285   1592   νCO + νCC + δCCN + a-in-plane-rd     1596   286   1592   νCO + νCC + δCCN + a-in-plane-rd     1628   296   1610   νCC + νCO + δCNC + a-in-plane-rd     1628   296   1610   νCC + νCO + δCNC + a-in-plane-rd     1628   296   1625   νCO + νCN + δCCN + a-in-plane-rd     1628   296   218   2968   s-νCH2     297   290   2965   s-νCH2     298   298   s-νCH2 + δCCN   νCC + νCN     217   2968   s-νCH2 + δCCN   νCC + νCN     218   2970   s-νCH2 + δCCN   νCC + νCN     292   2971   298   s-νCH2 + δCCN   νCC + νCN     298   298   s-νCH2 + δCCN   νCC + νCN     299   2995   s-νCH2 + δCCN   νCC + νCN     299   3138   s-ν-νCH + in-plane-rd     300   3140   s-	1044	1033			· · · · · · · · · · · · · · · · · · ·
1212   1213   619   1211   s-in-plane-rd + δCCN   1282   570   1267   δCCN + a-in-plane-rd   5588   1287   δCCN + a-in-plane-rd   549   1294   δCCN + a-in-plane-rd   549   1294   δCCN + a-in-plane-rd   532   1306   δCCN + a-in-plane-rd   532   1306   δCCN + a-in-plane-rd   532   1311   δCCN + a-in-plane-rd   521   1311   δCCN + a-in-plane-rd   521   1311   δCCN + a-in-plane-rd   521   1314   δCCNC   348   1354   ωCH2 + δCCN + a-in-plane-rd   340   1523   νCN + νCC   328   1533   νCN + νCC   328   1533   νCN + νCC   328   1533   νCN + νCC   331   1575   νCC + δCCN + in-plane-rd   286   1592   νCC + νCO + δCNC + a-in-plane-rd   286   1592   νCC + νCO + δCNC + a-in-plane-rd   286   1592   νCC + νCO + δCNC + a-in-plane-rd   260   1611   νCC + νCN + δCCN + s-in-plane-rd   260   1611   νCO + νCN + δCCN + s-in-plane-rd   260   1611   νCO + νCN + δCCN + s-in-plane-rd   232   1634   νCO + νCN + δCCN + a-in-plane-rd   232   1634   νCO + νCN + δCNC + a-in-plane-rd   232   1634   νCO + νCN + δCNC + a-in-plane-rd   243   3290   s-νCH2 + δCCN   νCO + νCN + δCNC + a-in-plane-rd   243   3290   s-νCH2 + δCCN + νCO + νCN   213   2970   s-νCH2 + δCCN + νCO + νCN   213   2970   s-νCH2 + δCCN + νCO + νCN   2984   s-νCH2 + δCCN + νCO + νCN					· · · · · · · · · · · · · · · · · · ·
1282   570   1267   δCCN + a-in-plane-rd   558   1287   δCCN + a-in-plane-rd   549   1294   δCCN + a-in-plane-rd   549   1294   δCCN + a-in-plane-rd   532   1306   δCCN + a-in-plane-rd   532   1306   δCCN + a-in-plane-rd   521   1311   δCCN + a-in-plane-rd   521   1311   δCCN + a-in-plane-rd   521   1311   δCCN + a-in-plane-rd   340   1523   $\nu$ CN + $\nu$ CC   348   1354   $\nu$ CH2 + $\nu$ CCN + a-in-plane-rd   340   1523   $\nu$ CN + $\nu$ CC   328   1533   $\nu$ CN + $\nu$ CC   328   1533   $\nu$ CN + $\nu$ CC   328   1533   $\nu$ CN + $\nu$ CC   301   1575   $\nu$ CC + $\nu$ CO + $\nu$ CN + a-in-plane-rd   286   1592   $\nu$ CC + $\nu$ CO + $\nu$ CN + a-in-plane-rd   285   1592   $\nu$ CC + $\nu$ CO + $\nu$ CN + a-in-plane-rd   285   1592   $\nu$ CC + $\nu$ CO + $\nu$ CN + a-in-plane-rd   260   1611   $\nu$ CC + $\nu$ CN + $\nu$ CC + a-in-plane-rd   260   1611   $\nu$ CC + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1611   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1612   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1613   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1614   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1615   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1616   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1617   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1618   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1619   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   260   1611   $\nu$ CO + $\nu$ CN + $\nu$ CCN + a-in-plane-rd   270   2905   $\nu$ CH2 + $\nu$ CCN + $\nu$ CN + a-in-plane-rd   271   2968   $\nu$ CH2 + $\nu$ CCN + $\nu$ CN + a-in-plane-rd   272   2968   $\nu$ CH2 + $\nu$ CCN + $\nu$ CN + $\nu$ CN + $\nu$ CN   273   2970   $\nu$ CCH + $\nu$ CN + $\nu$ CC + $\nu$ CN   2970   $\nu$ CCH + $\nu$ CN + $\nu$ CCH + $\nu$ CN   2970   $\nu$ CCH + $\nu$ CN + $\nu$ CCH + $\nu$ CN   2970   $\nu$ CCH + $\nu$ CN + $\nu$ CCH + $\nu$ CN   2970   $\nu$ CCH + $\nu$ CN + $\nu$ CCH + $\nu$ CN   2970	1202	1213			
1282		1306			<u> </u>
1301   1306   549   1294   δCCN + a-in-plane-rd   1306   537   1305   δCCN + a-in-plane-rd   1306   532   1306   δCCN + a-in-plane-rd   1312   519   1317   7CCNC   1314   491   1348   δCCNC   328   1333   $\nu$ CN + $\nu$ CC   $\nu$ CON + $\nu$ CC   328   1333   $\nu$ CN + $\nu$ CC   328   1333   $\nu$ CN + $\nu$ CC   331   1575   $\nu$ CC + $\nu$ CCN + in-plane-rd   286   1592   $\nu$ CC + $\nu$ CON + $\nu$ CC   287   286   1592   $\nu$ CC + $\nu$ CON + $\nu$ CC   287   261   1610   $\nu$ CC + $\nu$ CON + $\nu$ CC + $\nu$ CN + $\nu$ CN + $\nu$ CC + $\nu$ CN +	1282		558	1287	•
1306   537   1305   $\delta$ CCN + a-in-plane-rd     532   1306   $\delta$ CCN + a-in-plane-rd     521   1311   $\delta$ CCN + a-in-plane-rd     1322   519   1317   $\tau$ CCNC     1349   481   1348   $\delta$ CCNC     1360   1531   333   1529   $\nu$ CN + $\nu$ CC     328   1533   $\nu$ CN + $\nu$ CC     330   1575   $\nu$ CC + $\nu$ CO + $\nu$ CC + $\nu$ CO + $\nu$ CO     328   1539   $\nu$ CN + $\nu$ CC     329   $\nu$ CO +	í		549	1294	
1301   532   1306   δCCN + a-in-plane-rd   1322   519   1317   $r$ CCNC   1362   1349   481   1348   $r$ CCN + $r$ CCN   1363   1531   333   1529   $r$ CN + $r$ CCN   1370   1531   333   1529   $r$ CN + $r$ CC   1582   303   1575   $r$ CC + $r$ CCN + in-plane-rd   1582   303   1575   $r$ CC + $r$ CCN + in-plane-rd   1582   303   1575   $r$ CC + $r$ CCN + in-plane-rd   1584   286   1592   $r$ CC + $r$ CON + $r$ CN + $r$ CN   1599   1597   261   1610   $r$ CC + $r$ CON + $r$ CCN + a-in-plane-rd   1628   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1628   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1628   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1628   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1629   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1620   243   1620   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1621   232   1634   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1622   236   1625   $r$ CON + $r$ CN + $r$ CCN + a-in-plane-rd   1623   2370   2380   $r$ CCN + $r$ CCN + $r$ CN			537	1305	<u>-</u>
1322 519 1311 δCCN + a-in-plane-rd  1362 1349 481 1348 δCCNC  1360 1531 333 1529 $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1530 1531 333 1529 $\nu$ CN + $\nu$ CC  1582 303 1575 $\nu$ CC + s-in-plane-rd + $\nu$ CO  1582 286 1592 $\nu$ CC + $\nu$ CO + $\delta$ CCN + a-in-plane-rd  1594 286 1592 $\nu$ CC + $\nu$ CO + $\delta$ CCN + a-in-plane-rd  1595 261 1610 $\nu$ CC + $\nu$ CO + $\delta$ CNC + a-in-plane-rd  1628 262 1592 $\nu$ CO + $\nu$ CO + $\delta$ CNC + a-in-plane-rd  1628 1620 1611 $\nu$ CO + $\nu$ CN + $\nu$ CC + $\delta$ CCN + a-in-plane-rd  1628 1620 1611 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1625 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1625 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1625 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1626 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1626 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1627 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1628 1626 $\nu$ CO + $\nu$ CN + $\delta$ CCN + a-in-plane-rd  1629 270 2965 $\nu$ CH2  2970 2966 $\nu$ CH2 + $\delta$ CCN  2910 2966 $\nu$ CH2 + $\delta$ CCN  2911 2968 $\nu$ CH2 + $\delta$ CCN + $\nu$ CC + $\nu$ CN  2912 2969 $\nu$ CH2 + $\delta$ CCN + $\nu$ CC + $\nu$ CN  2913 2970 $\nu$ CH2 + $\delta$ CCN + $\nu$ CC + $\nu$ CN  2914 310 3105 $\nu$ CH2 + $\delta$ CCN + $\nu$ CC + $\nu$ CN  2915 3105 $\nu$ CH2 + $\delta$ CCN + $\nu$ CC + $\nu$ CN  2916 2917 2918 2919 2919 2919 2919 2919 2919 2919	1301				•
1322 519 1317 $r$ CCNC  1362 1349 491 1348 $δ$ CCNC  1363 1531 1523 $ν$ CN + $δ$ CCN + a-in-plane-rd  340 1523 $ν$ CN + $δ$ CCN  1530 1531 333 1529 $ν$ CN + $ν$ CC  328 1533 $ν$ CN + $ν$ CC  328 1533 $ν$ CN + $ν$ CC  310 1575 $ν$ CC + s-in-plane-rd + $ν$ CO  328 1533 $ν$ CN + $ν$ CC  300 1575 $ν$ CC + s-in-plane-rd + $ν$ CO  286 1592 $ν$ CC + $ν$ CO + $δ$ CNC + a-in-plane-rd  286 1592 $ν$ CC + $ν$ CO + $δ$ CNC + a-in-plane-rd  286 1592 $ν$ CC + $ν$ CO + $δ$ CNC + a-in-plane-rd  286 1592 $ν$ CO + $ν$ CC + $δ$ CCN + a-in-plane-rd  286 1592 $ν$ CO + $ν$ CN + $δ$ CCN + s-in-plane-rd  286 1625 $ν$ CO + $ν$ CN + $δ$ CCN + s-in-plane-rd  286 1625 $ν$ CO + $ν$ CN + $δ$ CCN + s-in-plane-rd  287 1620 1611 $ν$ CO + $ν$ CN + $δ$ CCN + s-in-plane-rd  288 1625 $ν$ CO + $ν$ CN + $δ$ CCN + s-in-plane-rd  289 1634 $ν$ CO + $ν$ CN + $δ$ CCN + a-in-plane-rd  290 2965 $ν$ νCH2  2919 2966 $ν$ νCH2  2919 2966 $ν$ νCH2 + $δ$ CCN  2110 2968 $ν$ νCH2 + $δ$ CCN  2111 2968 $ν$ νCH2 + $δ$ CCN + $ν$ CC + $ν$ CN  2112 2968 $ν$ νCH2 + $δ$ CCN + $ν$ CC + $ν$ CN  2113 2970 $ν$ νCH2 + $δ$ CCN + $ν$ CC + $ν$ CN  2927 202 2995 $ν$ νCH2 + $δ$ CCN + $ν$ CC + $ν$ CN  2948 3007 117 3114 $ν$ 115 $ν$ 1- $ν$ CH + a-in-plane-rd  3009 79 3138 $ν$ 1- $ν$ CH + in-plane-rd  3009 79 3138 $ν$ 1- $ν$ CH + in-plane-rd  3009 70 3139 $ν$ 1- $ν$ CH + in-plane-rd  3009 3140 $ν$ 1 317 $ν$ 1 $ν$ CH + in-plane-rd  30140 3141 $ν$ 1 $ν$			521	1311	•
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	1530	1531	340	1523	$\nu$ CN + $\delta$ CCN
			333	1529	$\nu \text{CN} + \nu \text{CC}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			328	1533	$\nu \text{CN} + \nu \text{CC}$
301   1575   νCC + δCCN + in-plane-rd			303	1575	$\nu$ CC + s-in-plane-rd + $\nu$ CO
		1597	301	1575	$\nu$ CC + $\delta$ CCN + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			286	1592	$\nu$ CC + $\nu$ CO + $\delta$ CNC + a-in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			285	1592	$\nu$ CO + $\nu$ CC + $\delta$ CCN + a-in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			276	1597	$\nu$ CC + $\nu$ CO + $\delta$ CNC + a-in-plane-rd
			261	1610	$\nu$ CC + $\nu$ CN + $\delta$ CCN + s-in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			260	1611	$\nu$ CO + $\nu$ CN + $\nu$ CC + $\delta$ CCN + s-in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1628		243	1620	$\nu$ CO + $\nu$ CC + $\nu$ CN+ $\delta$ CCN + s-in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			236	1625	$\nu \text{CO} + \nu \text{CN} + \delta \text{CCN} + \text{a-in-plane-rd}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			232	1634	$\nu { m CO} + \nu { m CN} + \delta { m CNC} + { m a-in-plane-rd}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2878	2968	220	2965	s-\(\nu\)CH2
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			219	2966	s- $\nu$ CH2 + $\delta$ CCN
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			218	2968	$s-\nu CH2 + \delta CCN + \nu CC + \nu CN$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			217	2968	$s-\nu CH_2 + \delta CCN + \nu CC + \nu CN$
			213	2970	$s-\nu CH_2 + \delta CCN + \nu CC + \nu CN$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2927		202	2995	$s-\nu CH_2 + \delta CCN + \nu CC + \nu CN$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ſ		134	3105	a-r- $\nu$ CH + a-in-plane-rd
	9049	3007	117	3114	s-r- $\nu$ CH
			115	3115	s-r- $\nu\mathrm{CH}$
			110	3118	r- $ u$ CH + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3009	3140	79	3138	s-r- $\nu$ CH + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			75	3138	s-r- $\nu$ CH + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			73	3139	r- $\nu {\rm CH}$ + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ſ		63	3146	s-r- $\nu$ CH + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3033{		54	3147	r- $\nu \mathrm{CH}$ + in-plane-rd
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			50	3147	r- $\nu$ CH + in-plane-rd
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			42	3151	r- $\nu {\rm CH}$ + in-plane-rd
3291 3310 31 3309 $\nu$ NH + $\nu$ CN + $\delta$ CNC 3322 3340 20 3340 $\nu$ NH + $\nu$ CN 8 3410 $\nu$ NH			38	3170	r- $\nu \mathrm{CH}$ + in-plane-rd
$31$ $3309$ $\nu NH + \nu CN + \delta CNC$ $3322$ $3340$ $20$ $3340$ $\nu NH + \nu CN$ $8$ $3410$ $\nu NH$	2001	2210	32	3309	$\nu$ NH + $\nu$ CN + $\delta$ CNC
8 3410 νNH	ə291 ——	331U	31	3309	$\nu$ NH + $\nu$ CN + $\delta$ CNC
3362 3410	3322	3340	20	3340	$\nu$ NH + $\nu$ CN
$5   3410   \nu NH + \nu CN$	3360	2/10	8	3410	$\nu { m NH}$
	5502	0410	5	3410	$\nu NH + \nu CN$

## Table 1. continued

"The assignment of the selected normal modes is given in terms of usual internal coordinates of vibration. They are ordered by decreasing contribution to the corresponding normal mode. Internal coordinates:  $\nu$ , stretching;  $\delta$ , in-plane bending;  $\pi$ , out-of-plane bending;  $\tau$ , torsion and  $\omega$  wagging. Additional labels: a, antisymmetric; r, benzene ring; rd, benzene ring deformation; s, symmetric.

the Supporting Information (Figure S1), including the discrete set of calculated eigenvalues.

Region (i) corresponds to the very low-energy range, typically associated with phonon modes and complex molecular vibrations based on collective oscillations involving most of the atoms in the unit cell. For this reason, a more detailed analysis of these complex modes in terms of normal coordinates is absent. This conclusion is supported by the inspection of the discrete set of normal models associated with the broad peaks observed in this region of the spectrum (see the Supporting Information). Besides, it is well-known that for low-energy modes, the relaxation times involved in vibrational processes play a crucial role in the construction of the spectrum, leading to a significant variability in widths of the peaks. Thus, a direct comparison at quantitative level between theory and experiment becomes too difficult. However, Figure 4a shows a good matching between  $\mu$ -Raman and calculated spectra at qualitative level.

In region (ii), a peak-by-peak comparison is indeed possible (see Figure 4b). According to our normal mode analysis, this region is governed by skeletal modes preferentially involving not only the aromatic rings but also the bridging aliphatic chains. These modes include slight planar and nonplanar ring deformations and especially strong centrosymmetric in-plane vibrations, resembling the typical benzene breathing mode. Notice how the most intense peak in this region corresponds to these latter modes at ~1000 cm<sup>-1</sup> in combination with the lowest energetic stretching modes in the benzene rings.

Region (iii), which includes the wavenumber shifts between 1100 and 1700 cm<sup>-1</sup>, is the region which contains the largest amount of information in Raman spectroscopy and therefore involves the largest number of Raman active modes. As it is observed in Table 1, there are still present some modes associated with the rings, mainly antisymmetric in-plane distortions, leading to a strong band in the spectrum around 1300 cm<sup>-1</sup>, in combination with in-plane CCN vibrations. However, in this region, we have other typical vibration modes like torsion or CH<sub>2</sub> wagging, responsible for one strong peak at ~1350 cm<sup>-1</sup>. For higher wavenumber shifts in this region, benzene ring vibrations become progressively less prominent in favor of more energetic stretching modes of CN and CO, located at ~1530 and ~1600 cm<sup>-1</sup>, respectively (see Figure 4c). This fact is in good agreement with previous experimental evidence in which a systematic shift of these bands depending on the presence of different cations is demonstrated.<sup>11</sup> Because they come from strong polar bonds, it is expected a high interaction with ions via hydrogen bonds. Therefore, a high chemical sensitivity to the environment is displayed.

Last, region (iv) corresponds to the most energetic vibrations >2900 cm<sup>-1</sup>. Note in Figure 4d that here a slight discrepancy between calculated eigenfrequencies and experimental peaks is found. As it can be seen, the shape of both renormalized spectra is the same but a displacement between 50 and 80 cm<sup>-1</sup> is found between both sets of peaks in Figure 4d. However, in this high-energy region of the spectrum, such differences in Raman shifts represent in the worse cases less than a 3% of uncertainty in the determination of the eigenfrequencies. Thus, we can still consider an accuracy level sufficient to proceed with the assignment. This region is essentially characterized by two different kinds of stretching vibrations: a strong stretching of CC in the aromatic rings located at [2900–3000] cm<sup>-1</sup> and the stretching of NH bonds located at [3300–3400] cm<sup>-1</sup>.

In summary, in this work, we have carried out the assignment of the observed Raman bands of benzylic amide

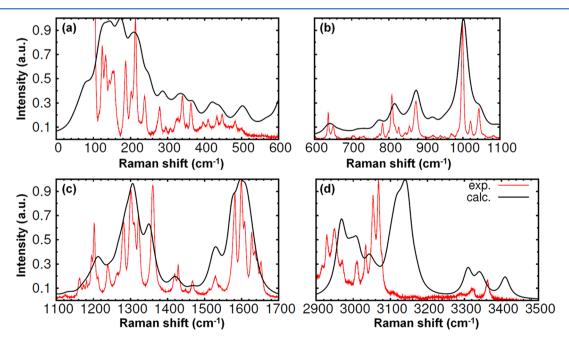


Figure 4. Comparison between the calculated Raman spectrum (black line) and the experimental averaged spectrum (red line) after renormalization in different wavenumber regions. See text for further details.

[2] catenane, which establishes a fundamental and useful basis for future studies on interactions, reactions, and structural alterations of this compound by vibrational spectroscopy. Furthermore, this band assignment based on the geometrical description of most relevant normal modes involved could be very helpful in further spectroscopic studies of related compounds.

## 5. CONCLUSIONS

In this work, we have performed a comprehensive characterization of the Raman spectrum of solid-state benzylic amide [2] catenane by means of  $\mu$ -Raman experiments and firstprinciples calculations. Despite the complexity of this compound, the agreement found between experimental spectra and calculations is excellent, which allows us to carry out the complete assignment of the main vibrational modes responsible for the Raman spectrum. Additionally, a detailed geometrical description of these modes in terms of the usual normal coordinates is provided. Furthermore, these findings about the molecular structure of this compound could be of great interest in further studies involving the interaction of other mechanically interlocked molecules with their chemical environment or subsequent characterization works using spectroscopic techniques. Finally, the computational approach devised in this work is completely applicable to other systems expecting results with a similar accuracy.

## ASSOCIATED CONTENT

# **S** Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.8b04904

A complete study of the normal modes of the benzamide molecule and supplementary figures of the Raman spectra (PDF)

Animated visualizations of each mode are possible using standard softwares like Jmol, Avogadro, etc. A set of files (.xyz) with the coordinates of the normal modes collected in Table 1 is provided (ZIP)

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#### Notes

The authors declare no competing financial interest.

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## ABBREVIATION

DFT, density functional theory; NMR, nuclear magnetic resonance

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